

## EOS Summary

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#### 1. HELMHOLTZ EOS

These will be notes condensed from [Timmes & Swesty \(2000\)](#)

They got an electron-positron equation of state based on table interpolation of Helmholtz free energy using biquintic Hermite polynomials. Direct evaluation of the EOS would be time consuming as over  $10^9$  calls will be made in a 2D or 3D hydrodynamical simulation. However table interpolation has to be done with enough resolution and should be thermodynamically consistent (i.e. satisfy Maxwell's equations) [Eq 2,3 and 4 in [Timmes & Swesty \(2000\)](#)]

*Thermodynamic inconsistency may manifest itself in the unphysical buildup (or decay) of the entropy (or temperature) during numerical simulations of what should be an adiabatic flow.* [Timmes & Swesty \(2000\)](#)

$$F = E - TS, \quad dF = SdT - \frac{P}{\rho^2}d\rho \quad (1)$$

With this definition of Helmholtz Free energy if we define our pressure and entropy as:

$$P = \rho^2 \left. \frac{\partial F}{\partial \rho} \right|_T \quad (2)$$

$$S = - \left. \frac{\partial F}{\partial T} \right|_\rho \quad (3)$$

we can interpolate a give  $F(\rho, T)$  table with any interpolating function (which lets derivatives of density and temperature commute) and it will be thermodynamically consistent, however wrong the interpolation maybe.

#### 2. SECTION 2

Lorem Ipsum

#### REFERENCES

Timmes, F. X., & Arnett, D. 1999, ApJS, 125, 277,  
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